

Institut d'Optique

CNRS CENTRE NATIONAL DE LA RECHERCHE SCIENTIFIQUE

Atomic mirrors, atom lasers, and BECs from incoherent to quantum atom optics

Groupe d'Optique Atomique
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<http://atomoptic.institutoptique.fr>

Atomic mirrors, atom lasers, and BECs

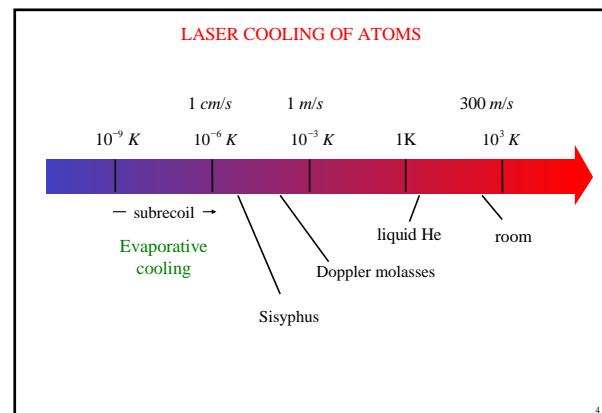
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Ray Optics, Wave optics, Quantum Optics
2. Atomic mirrors: incoherent and coherent atom optics
 1. Classical reflection: a probe of the atom wall interaction
 2. Coherent atom optics with incoherent atom sources: matter wave diffraction
 3. Why coherent optics with a coherent source (a laser) ?
3. Bose-Einstein Condensates and Atom lasers
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Atom Optics

Do with atoms what standard optics does with photons :

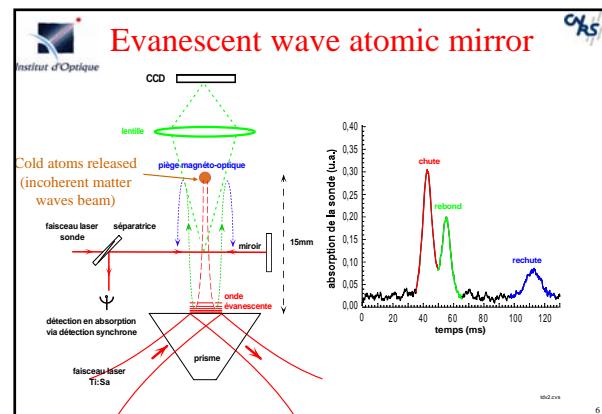
- Reflection, refraction, focusing: **geometrical optics** (incoherent)
- Trajectories \longleftrightarrow Rays
- Interference, diffraction: **wave optics** (coherent)
- Matter Waves \longleftrightarrow Electromagnetic Waves
- Wave/particle, squeezing, entanglement: **quantum optics**
- Atoms (as quanta of matter waves) \longleftrightarrow Photons (quanta...)

Possible because of progress in control of atomic motion



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Interaction atome paroi à courte distance

Dipôle électrostatique interagissant avec son image dans un conducteur diélectrique

$$U(z) = -\frac{1}{64\pi\epsilon_0} \frac{d_x^2 + d_y^2 + 2d_z^2}{z^3} \frac{\epsilon - 1}{\epsilon + 1}$$

Lennard-Jones : atome dans son état fondamental

$$d^2 \rightarrow \langle g | \hat{D}^2 | g \rangle = \sum_i \langle g | \hat{D} | e_i \rangle^2 \neq 0$$

Fluctuations du dipôle atomique dominées par la première transition de résonance ω_l

\Rightarrow Effets de retard négligeables si $z \ll \frac{c}{\omega_l} \approx 100 \text{ nm}$

Potentiel de Casimir-Polder (atome-métal)

Calcul d'électrodynamique quantique valable à toute distance

$$U_{CP}(z) \xrightarrow{z \rightarrow \infty} -\frac{3}{32\pi^2\epsilon_0} \frac{\hbar c \alpha}{z^4}$$

α : polarisabilité statique, dominée par ω_l

Interprétation (analogie Casimir entre conducteurs [10]: Haroche)

- déplacement du niveau fondamental (Lamb shift) dû aux fluctuations du vide
- valeur dépend de la structure des modes autour de l'atome
- modes affectés par le conducteur $\omega_l < \frac{c}{z}$

Remarque : z grand $\Rightarrow \omega_l \ll \omega_l \Rightarrow$ polarisabilité statique

Potentiel de Lifshitz (atome-diélectrique)

$U_L(z) \xrightarrow{z \rightarrow \infty} U_{CP}(z) \frac{\epsilon(\omega_l) - 1}{\epsilon(\omega_l) + 1} \phi(\epsilon)$

$\phi(\epsilon) = 0.77$ pour $1 < \sqrt{\epsilon} < 2$
 $\phi(\epsilon) \approx 1$ pour $\epsilon \rightarrow \infty$ (métal)

A courte distance: Lennard Jones avec indice

Interaction atome – diélectrique dans un miroir atomique (Orsay, 1996)

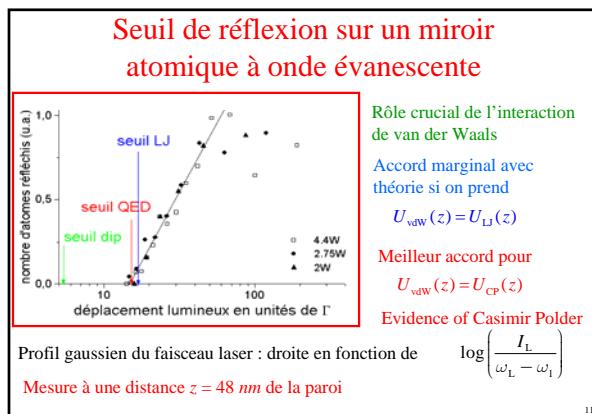
rebond, chute, rebute, Réflexion sur onde évanescante

$U_{dip} = \hbar \Lambda e^{-2\kappa z}$

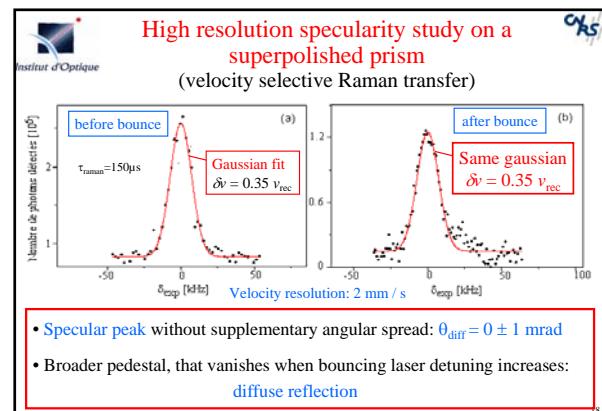
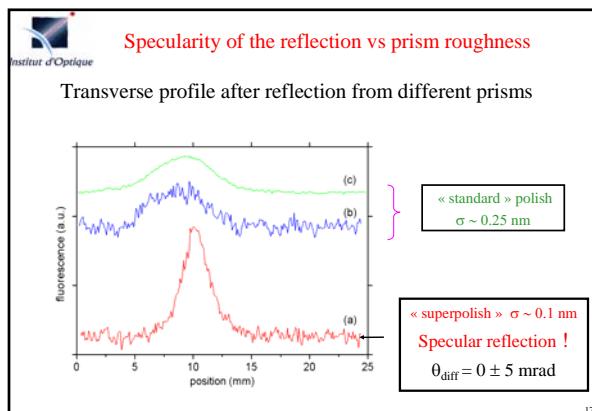
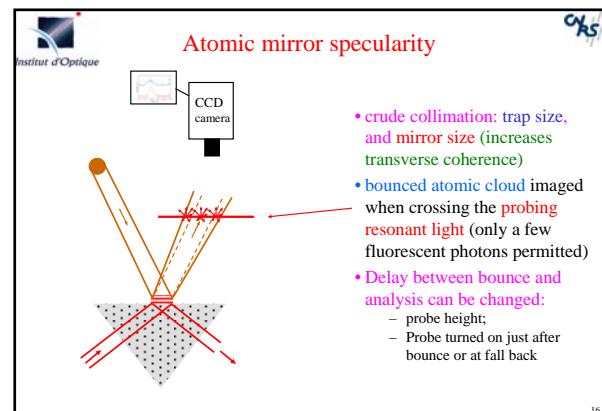
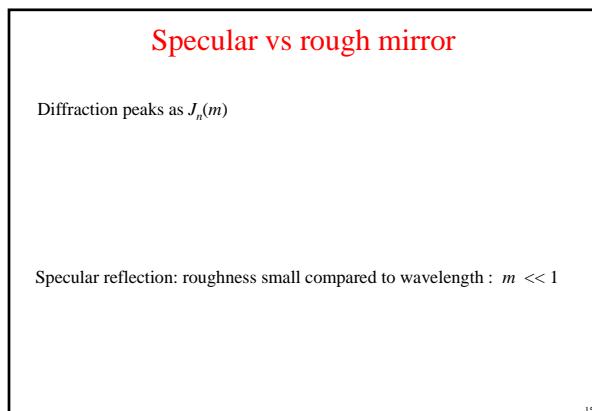
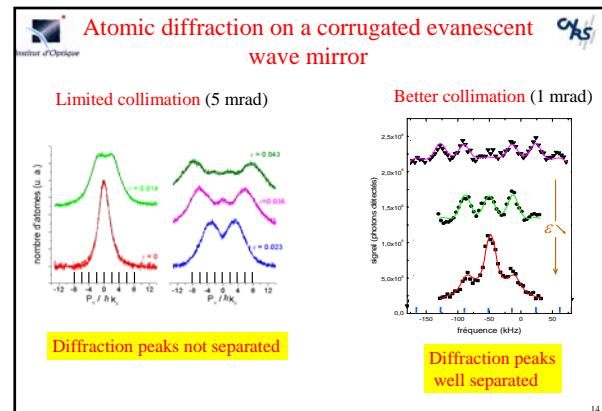
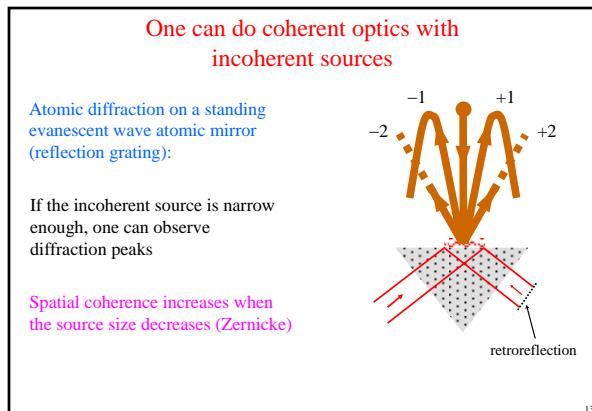
Potentiel réflecteur

Potentiel反映了 par les paramètres du laser onde évanescante (intensité, désaccord à résonance) :

\Rightarrow seuil de réflexion pour énergie incidente Mgh définie (atomes froids)
 \Rightarrow potentiel de van der Waals au seuil de réflexion



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Specular reflection on imperfect mirrors?

How can a real mirror, with some unavoidable residual roughness, behave as an ideally flat reflector?

Because it reflects waves

If wavelength $\lambda \gg$ roughness σ

$$\Rightarrow \text{Diffuse reflection vanishes as } 1 - \exp\left(-\frac{\sigma^2}{2\pi^2 \lambda^2}\right)$$

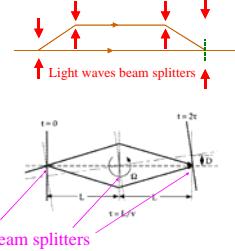
\Rightarrow Specular reflection: preserves coherence

Analogous to Debye-Waller, Mössbauer, Lamb-Dicke effects

Interferometry with large incoherent sources

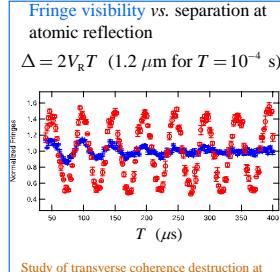
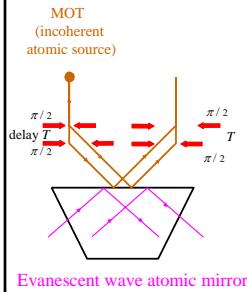
As in photon optics, large size incoherent sources can yield high visibility fringes in Michelson-like (or Mach-Zehnder like) atom interferometers :

- Field amplitude division (beam splitters)
- Fringe « localized » in a particular plane



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An atomic mirror interferometer with a large incoherent source



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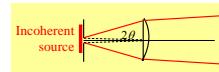
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The limits of optics with incoherent source

Incoherent optics can achieve high precision measurements of position, direction...

- Requires filtering (for instance collimation)
 \Rightarrow coherence increases
- Ultimately: selection of a single mode: $\Delta x \cdot \Delta \theta = 1$ (coherence)



Filtering \Rightarrow weak signal. Much less than one photon per mode

Analogous problem in atom optics : cooling and trapping typically yields 10^{-6} atom per phase space elementary cell $\Delta^3 r \cdot \Delta^3 p = \hbar^3$

THE solution in photon optics: LASER
many photons per mode ($> 10^{10}$ for a simple He-Ne laser)

In atom optics: Atom laser ? Many atoms in \hbar^3 ?

How to have many atoms in the same mode ?

Bose-Einstein Condensation:

- \Rightarrow happens when atomic wave packets overlap $n \Lambda_T^3 \geq 1$
- \Rightarrow increase of density usually leads to molecule (or cluster) formation (except liquid Helium: superfluidity)
- \Rightarrow At temperature below 1 μK , BEC with dilute atomic medium

First demonstration in 1995 : evaporative cooling of magnetically trapped alkali atoms (Rb, Na, Li) : Boulder, MIT, Rice

Nobel 2001

BEC of spin polarized hydrogen (MIT, 1998)

BEC of metastable helium (Institut d'Optique, ENS, 2001)

BEC in an optical trap (Georgiatech, 2001)

More alkali: K (Florence 2001).

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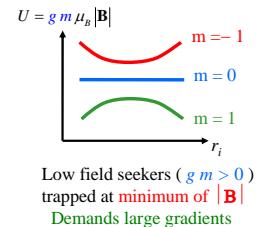
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Recipe for BEC with a dilute atomic sample

- $n \Lambda_T^3 \geq 1 \implies$ decrease temperature and/or increase density (moderately)
- Laser cooling and trapping $\Rightarrow n \Lambda_T^3 \leq 10^{-6}$ (start from 10^{-15})
 - Turn off lasers (avoid rescattering, light induced inelastic collisions..)
 - Turn on a magnetic trap, with a non nul (bias) minimum magnetic field (avoid Majorana non adiabatic losses)
 $n \Lambda_T^3 < 10^{-6}$



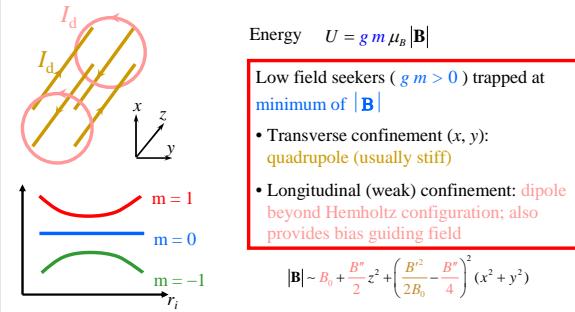
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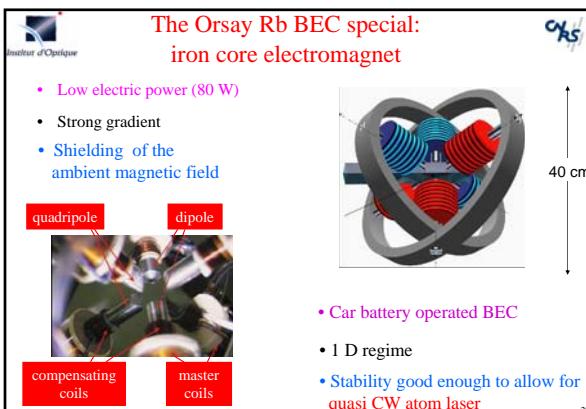
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Magnetic Trapping of paramagnetic atoms



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Recipe for BEC with a dilute atomic sample

- $n \Lambda_T^3 \geq 1 \implies$ decrease temperature and/or increase density (moderately)
- Laser cooling and trapping $\Rightarrow n \Lambda_T^3 \approx 10^{-6}$ (start from 10^{-15})
 - Turn off lasers (avoid rescattering, light induced inelastic collisions..)
 - Turn on a magnetic trap, with a non nul (bias) minimum magnetic field minimizing entropy increase (match potential) $n \Lambda_T^3 < 10^{-6}$
 - Forced (RF transition) evaporative cooling
 $\Rightarrow T$ decreases and $n \Lambda_T^3$ increases to 2.6...

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Forced evaporative cooling

$m = -1$

$k_B T$

U_0

$\hbar \Omega_{RF}$

RF eliminates atoms with energy $> \eta k_B T$ (typically $\eta \approx 6$)

After rethermalization (elastic collisions)

- $T \searrow \Rightarrow \Delta_T \nearrow$
- $n \nearrow$ (although $N \searrow$, because $T \searrow$)

 $\Rightarrow n \Delta_T^3 \nearrow$

Ω_{RF} ramped down to BEC

$n \Delta_T^3 > 2.612$

Strong demands

- large elastic cross section
- small losses ($< 1/300$ el.)
- background pressure ultra low
- no inelastic processes

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Optical observation of Rb condensation

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- Turn off the trap at $t = 0$
- Ballistic expansion, duration τ
- Absorption imaging
- Velocity distribution
 - * Thermal component (Gaussian wings)
 - * Condensate (inverted parabola)

$\approx 10^5 Rb$ atoms

ρ

V_x

V_y

200 nK

150 nK

< 100 nK

Measurement difficult for less than 10^4 atoms

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Non ideal (interacting) BEC

Non linear Schrödinger equation (Gross Pitaevskii equ.)

$$-\frac{\hbar^2}{2M} \Delta u_0(\mathbf{r}) + V(\mathbf{r})u_0(\mathbf{r}) + N g |u_0(\mathbf{r})|^2 u_0(\mathbf{r}) = \mu u_0(\mathbf{r})$$

\ Mean field interaction

Thomas Fermi approximation

$$-\frac{\hbar^2}{2M} \Delta u_0(\mathbf{r}) + V(\mathbf{r})u_0(\mathbf{r}) + N g |u_0(\mathbf{r})|^2 u_0(\mathbf{r}) = \mu u_0(\mathbf{r})$$

~~$-\frac{\hbar^2}{2M} \Delta u_0(\mathbf{r})$~~

Inverted parabola in a harmonic trap

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Interferences between BECs

Observation of Interference Between Two Bose Condensates

M. R. Andrews, C. G. Townsend, H.-J. Miesner, D. S. Durfee, D. M. Kurn, W. Ketterle

Interference between two freely expanding Bose-Einstein condensates has been observed. Two condensates separated by ~40 micrometers were created by evaporatively cooling sodium atoms in a double-well potential formed by magnetic and optical forces. High-contrast interference fringes with a period of ~15 micrometers were observed. The interference pattern was the same for the two condensates, which were separated for 40 milliseconds and overlapped. This demonstrates that Bose condensed atoms are "laser-like"; that is, they are coherent and show long-range correlations. These results have direct implications for the atom laser and the Josephson effect for atoms.

SCIENCE • VOL. 275 • 31 JANUARY 1997

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Rb quasi CW gravity driven atom laser

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Energy level diagram showing a double-well potential with energy E. The ground state levels are labeled $m = -1$ and $m = 0$. A red arrow labeled $\hbar\omega_{RF}$ indicates the detuning from the $m = 0$ level. A black arrow labeled g indicates the gravitational field along the z-axis.

Remaining condensate in $m = -1$ (separated by Stern-Gerlach)

RF (weak) outcoupler from BEC: falling single mode matter wave
cf. Esslinger et al.;
for a simple analytical 3D theory including gravity see Gerbier et al., PRL 2001

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Atom lasers

Transverse structure: the M^2 factor

J.-F. Riou et al., 2005

A guided atom laser

W. Guérin et al., 2006

Mode locked

"CW"

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Mode locked atom laser

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Comb of coherent RF outcoupplers

Energy level diagram showing a double-well potential with energy E. The ground state levels are labeled $m = -1$ and $m = 0$. Multiple green arrows labeled $\hbar\omega_{RF}$ indicate the detuning from the $m = 0$ level. A black arrow labeled g indicates the gravitational field along the z-axis.

Interference between coherent lasers at different frequencies: analogy to mode locked laser (cf Kasevich et al.)

BEC

Thermal cloud

FM = 200 Hz

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Divergence of a cw atom laser

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Divergence due to a lensing effect (interaction with the condensate)

Quantitatively interpreted with a straightforward extension of the ABCD matrices treatment of the propagation of usual (photon) laser beams

Divergence clearly increases with height z_{out} of the RF knife

ABC matrices (no adjustable parameter)

Divergence (mrad)

Outcoupler frequency (kHz)

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Coherent Atom Optics has much to learn from Coherent Photon Optics

- Do not forget your Optics classes
- There is a whole host of useful concepts, models, approximations...

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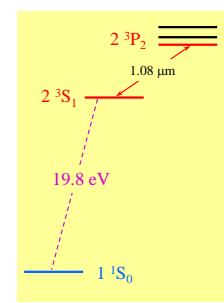
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Metastable Helium 2^3S_1

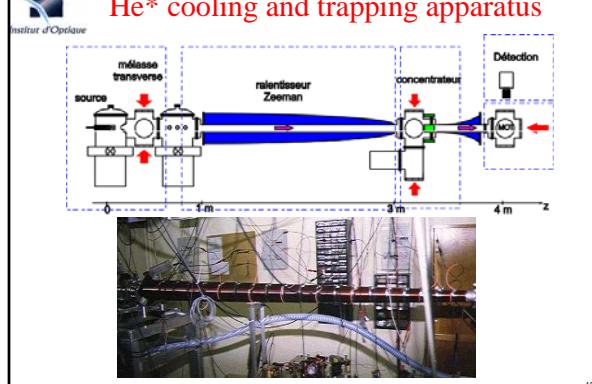
- Triplet ($\uparrow\uparrow$) 2^3S_1 cannot radiatively decay to singlet ($\downarrow\downarrow$) 1^1S_0 (lifetime 9000 s)
- Laser manipulation on closed transition $2^3S_1 \rightarrow 2^3P_2$ at 1.08 μm (lifetime 100 ns)

- Large electronic energy stored in He*
- ⇒ ionization of colliding atoms or molecules
- ⇒ extraction of electron from metal: single atom detection with Micro Channel Plate detector



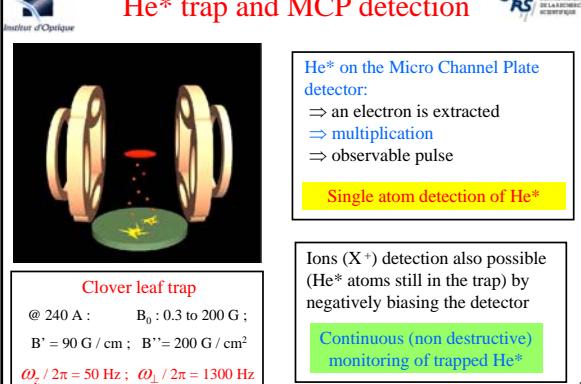
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He* cooling and trapping apparatus



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He* trap and MCP detection



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The route to He* BEC: not such an easy way

Pros:

- Strong magnetic trap (2 Bohr magnetons)
- Ultrasensitive detection scheme ⇒ Excellent TOF diagnostic
- Very rapid release scheme

Cons:

- Source of cold He* not as simple as alkalis'; vacuum challenges
- Penning ionization
- Elastic cross section unknown at low temperature

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Problem 1: Penning ionization of He*



Reaction constant $\approx 5 \times 10^{-10} \text{ cm}^3 \cdot \text{s}^{-1}$ @ 1 mK

Impossible to obtain a sample dense enough for fast thermalization?

Solution (theory, Shlyapnikov et al., 1994; Leo el al.):

Penning ionization strongly suppressed (10^{-5} !) in spin polarized He* because of spin conservation:

$$m = 1 + m = 1 \quad \cancel{\times} \quad s = 0 + s = 1/2 + s = 1/2$$

Magnetically trapped He* is spin polarized

Preliminary experimental evidence (Amsterdam, Orsay, 1999): suppr. $< 10^{-2}$

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Problem 2: thermalization

- Evaporative cooling requires a fast enough thermalization
- Initial density is small (large Penning ionization in Magneto-Optical Trap and optical molasses from which magnetic trap is loaded)
- ⇒ Fast thermalization demands large elastic collision cross section

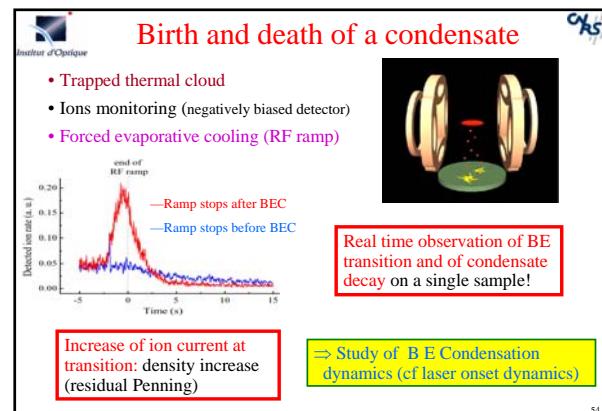
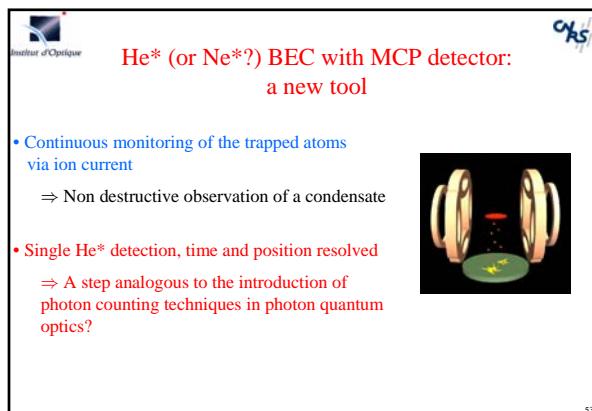
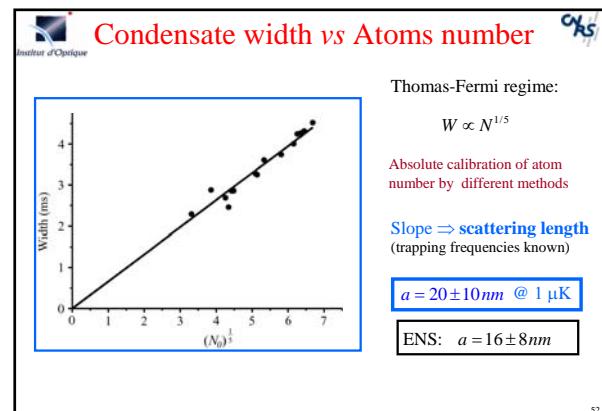
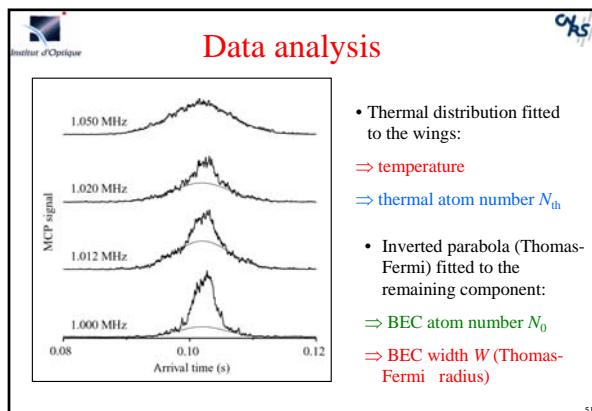
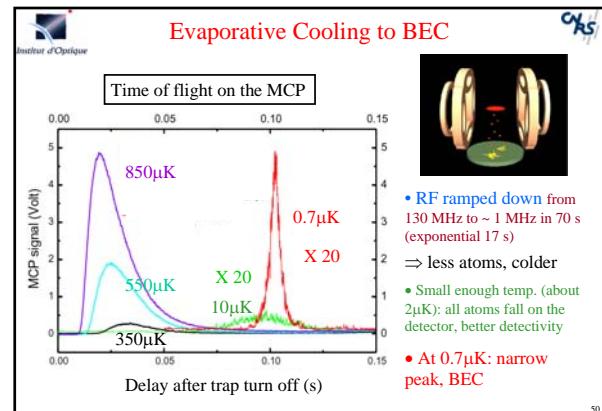
Encouraging calculations (Shlyapnikov 95, NIST): $a \approx 10 \text{ nm}$

Very encouraging measurements (Orsay, dec 2000, Browaeys et al, PRA)

- Direct measurement of thermalization of the energy distribution: $a \approx 20 \text{ nm}$
- Magnetic trap lifetime $\approx 1 \text{ mn}$

⇒ *elastic* > 300 criterium for evaporative cooling fulfilled

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New studies in quantum atom optics

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- A milestone in Photon Quantum Optics: the use of photon counters to measure photon statistics
- A similar step in Atom Optics: BEC of metastable atoms, single atom (or ion) detection resolved in space and time

• Study of correlation functions of atomic field

- Hanbury-Brown & Twiss type experiments
- Fluctuations of atom laser around BEC transition
- Build up of interferences from independent BEC
- Quantum optics with a small number of quanta...

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